The Equilibrium Constant K_p

- If all components are gases at constant temperature and volume, it may be more convenient to express the amounts of reactants and products in partial pressures.
 - T This is a variation on Gay-Lussac's Law of Combining Gas Volumes, based on the relationship P = gn, where g = f(V, T).
 - T For the Haber process at equilibrium:

$$N_2(g) + 3H_2(g) \circ 2NH_3(g)$$

In terms of partial pressures, we define the equilibrium constant K_p as

$$K_p = \frac{(p_{\rm NH_3})^2}{(p_{\rm N_2})(p_{\rm H_2})^3}$$

Relationship Between K_p and K_c

• For any gas species X,

$$p_{\rm X} = (n_{\rm X}/V)RT = [{\rm X}]RT$$

• For $N_2(g) + 3H_2(g) \circ 2NH_3(g)$, we can write

$$K_{p} = \frac{([\mathrm{NH}_{3}]RT)^{2}}{([\mathrm{N}_{2}]RT)([\mathrm{H}_{2}]RT)^{3}} = \frac{[\mathrm{NH}_{3}]^{2}}{[\mathrm{N}_{2}][\mathrm{H}_{2}]^{3}}(RT)^{-2}$$
$$K_{p} = K_{c}(RT)^{-2}$$

T Notice that the exponent on the *RT* term is the difference between the sum of coefficients on gas products minus the sum of coefficients on gas reactants:

) n = (2) - (1 + 3) = -2

L In general, the relationship between K_c and K_p is expressed by the equation

$$K_p = K_c (RT)^{n}$$

Examples of K_p and K_c

2NO₂(g) ° N₂O₄(g))
$$n = 1 - 2 = -1$$

 $K_p = K_c (RT)^{-1}$

 $H_2(g) + I_2(g) \circ 2HI(g)$) n = 2 - 2 = 0

$$K_p = K_c$$
 7 Note!

 $CaO(s) + CO_2(g) \circ CaCO_3(s)$

)
$$n = 0 - 1 = -1$$

 $K_p = K_c (RT)^{-1}$

The Reaction Quotient, Q

- We can calculate the ratio of concentrations or pressures like K_c or K_p at any time in course of a reaction.
- L When the system is *not at equilibrium*, the ratio of the product concentrations raised to their stoichiometric coefficients to the reactant concentrations raised to their stoichiometric coefficients is called the *reaction quotient* and given the symbol Q.
- L The value of Q relative to K_c or K_p indicates the direction in which the reaction must run to achieve equilibrium.
 - U If Q < K, the reaction must run in the forward direction, using up reactants and forming more products.

rR WpP $Q = [P]^{p}/[R]^{r} < K$ Y Shift right.

U If Q > K, the reaction must run in the reverse direction, using up products and reforming more reactants.

rR WpP
$$Q = [P]^{p}/[R]^{r} > K$$
 Y Shift left.

LeChatelier's Principle Henri LeChatelier - 1884

- L If a stress is applied to a system at equilibrium, the system will tend to adjust to a new equilibrium, which minimizes the stress, if possible.
 - Possible stresses are changes in T Concentration
 - T Pressure
 - T Temperature.

Shifts in the Position of Equilibrium

• Shift to the right:

Reactants ° Products

More reactants consumed, resulting in greater product concentrations and lesser reactant concentrations.

• Shift to the left:

Reactants ° Products

》

More products consumed, resulting in greater reactant concentrations and lesser product concentrations.

• Sometimes the stress cannot be alleviated by either kind of shift, in which case the original equilibrium position is maintained.

Reactants ° Products

° »

Effects of Various Stresses

- Concentration Change:
 - T Position of equilibrium changes
 - T K_c remains the same
- Pressure Change:
 - T Position of equilibrium *may* change
 - T K_c remains the same
- Temperature Change:
 - T Equilibrium changes
 - T K_c changes

Effects of Concentration Changes Reactants ^o Products

- Increase Reactant Concentrations

 Shift Right (more products)
- Increase Product Concentrations
 » Shift Left (more reactants)
- Remove Products as Formed

^o Shift Right (more products)

Effects of Pressure Changes) *n* ...0

- L If the sums of the coefficients of gas species in the balanced reaction equation are different between reactants and products () $n \dots 0$), an increase in pressure will cause a shift toward the side with the lower sum of coefficients.
 - This creates fewer gas molecules in the mixture, which reduces the total pressure $(P_t = n_t RT/V)$.

 $2NO_{2}(g) \circ N_{2}O_{4}(g)$ Increase $P \circ$ shift right $N_{2}(g) + 3H_{2}(g) \circ 2NH_{3}(g)$ Increase $P \circ$ shift right $2C(s) + O_{2}(g) \circ 2CO(g)$ Increase $P \otimes$ shift left $H_{2}O(g) + C(s) \circ H_{2}(g) + CO(g)$ Increase $P \otimes$ shift left

Effects of Pressure Changes) n = 0

L If the sums of gas species coefficients are the same on both sides of the equation () n = 0), pressure will have no effect on the position of the equilibrium; e.g.,

> $N_2(g) + O_2(g) \circ 2NO(g)$ $H_2(g) + I_2(g) \circ 2HI(g)$ $C(s) + O_2(g) \circ CO_2(g)$

Effects of Temperature Changes

- L Changing temperature changes the value of K_c .
- If we know whether the reaction is exothermic or endothermic we can predict the *qualitative* effect of a temperature change.
 - T Raising the temperature will cause a shift that uses some of the added heat; i.e., added heat drives the endothermic process.

 $2NO_2(g) \circ N_2O_4(g) + heat$

Increase T • Y more NO₂, decrease K_c – Decrease T – Y more N₂O₄, increase K_c •

heat + $CO_2(g)$ + $H_2(g)$ ° CO(g) + $H_2O(g)$

Increase T • Y more products, increase K_c • Decrease T - Y more reactants, decrease K_c -

Effect of a Catalyst

- L A catalyst has no effect on equilibrium.
- L The catalyst offers an alternative path to products, but it does not affect the ratio of products to reactants at equilibrium.
- L The catalyst merely influences the rate at which equilibrium will be established.