

Summary of Calculations for Weak Acid and Weak Base Titrations

Region	HA titrated with OH ⁻	B titrated with H ₃ O ⁺
Initial (no added titrant)	$K_a = \frac{[\text{H}_3\text{O}^+]^2}{[\text{HA}]}$ $= \frac{[\text{H}_3\text{O}^+]^2}{C_{\text{HA}} - [\text{H}_3\text{O}^+]}$ <p>Often, $[\text{H}_3\text{O}^+] = \sqrt{K_a C_{\text{HA}}}$</p>	$K_b = \frac{[\text{OH}^-]^2}{[\text{B}]}$ $= \frac{[\text{OH}^-]^2}{C_{\text{B}} - [\text{OH}^-]}$ <p>Often, $[\text{OH}^-] = \sqrt{K_b C_{\text{B}}}$</p>
Before Equivalence Point (Buffer Region)	$K_a = \frac{[\text{H}_3\text{O}^+] C_{\text{A}^-}}{C_{\text{HA}}}$ $[\text{H}_3\text{O}^+] = K_a \times \left(\frac{\text{mmol HA}}{\text{mmol A}^-} \right)$	$K_b = \frac{[\text{OH}^-] C_{\text{BH}^+}}{C_{\text{B}}}$ $[\text{OH}^-] = K_b \times \left(\frac{\text{mmol B}}{\text{mmol BH}^+} \right)$
Half Titration Point	$[\text{A}^-] = [\text{HA}]$ $[\text{H}_3\text{O}^+] = K_a$ $\text{pH} = \text{p}K_a$	$[\text{BH}^+] = [\text{B}]$ $[\text{OH}^-] = K_b$ $\text{pOH} = \text{p}K_b$
Equivalence Point	$K_b^{\text{A}^-} = \frac{K_w}{K_a^{\text{HA}}}$ $[\text{OH}^-] = \sqrt{K_b^{\text{A}^-} C_{\text{A}^-}}$	$K_a^{\text{BH}^+} = \frac{K_w}{K_b^{\text{B}}}$ $[\text{H}_3\text{O}^+] = \sqrt{K_a^{\text{BH}^+} C_{\text{BH}^+}}$
After Equivalence Point	$[\text{OH}^-] = \left(\frac{\text{mmol excess OH}^-}{\text{total volume}} \right)$	$[\text{H}_3\text{O}^+] = \left(\frac{\text{mmol excess H}_3\text{O}^+}{\text{total volume}} \right)$